respectively 0.024 Å and -0.060 Å out of this plane; this is partly because the carboxylic group makes a small angle of 3.3° with the benzene ring plane and may partly be due to the fact that the oxygen atoms are drawn towards the centre of the dimer, presumably because of the force exerted by the hydrogen bonds. This is indicated by the unequal distances of the two oxygen atoms from the benzene ring plane and by the fact that the distance of the centre of the dimer from the plane of the carboxylic group (-0.047 Å) is less than its distance from the benzene ring plane(-0.118 Å).

The observed value of 1.501 Å for the exocyclic C-C bond length is the expected single bond distance between the carbon atoms in sp^2 states of hybridization. This indicates that there is no appreciable degree of conjugation across this bond; this fact again suggests that as expected, there is no contribution from quinonoid valence bond structure in *p*-nitrobenzoic acid.

The nitrogen atom N is -0.047 Å out of the plane of the benzene ring. The atom C(4) is 0.121 Å away from the plane of the nitro group; the angle between this and the benzene ring plane is 13.7°. The C-N bond length of 1.480 Å is significantly longer than the corresponding bond lengths in *p*-nitroaniline (1.460 Å), α -p-nitrophenol (1.442 Å) and β -p-nitrophenol (1.450 Å). The mean of the two N-O bond lengths in p-nitrobenzoic acid is 1.216 Å. In *p*-nitroaniline and β -*p*-nitrophenol, the corresponding lengths after correction for thermal motion are 1.247 Å and 1.242 Å respectively. There is pronounced torsional oscillation of the nitro group in these latter structures and the correction for torsional effects in N-O distances is about 0.018 Å. In the present study, anisotropic thermal parameters have not been obtained; however, the individual isotropic temperature factors for the oxygen atoms of the nitro group (Table 1) are not much larger than the values for other atoms; there is thus no suggestion of pronounced torsional oscillation of the nitro group. It thus appears that the N-O bonds in *p*-nitrobenzoic acid are significantly shorter than those in *p*-nitroaniline and *p*-nitrophenol. The shortening of the N-O bonds and the elongation of the C-N bond in *p*-nitrobenzoic acid from the corresponding values in *p*-nitroaniline and *p*-nitrophenol further supports the view that the bond length variations are due to minor contributions from quinonoid valence bond structures in the latter compounds.

The arrangement of molecules in the unit cell is shown in Fig.2, in which the principal intermolecular distances are also shown.

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Refinement of the Structure of Cd(NO₃)₂.4H₂O

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The crystal structure of $Cd(NO_3)_2.4H_2O$ has been refined by least-squares calculations to a final R index of 8.4%. The estimated standard deviations of atomic coordinates ranged from 0.0005 to 0.0042. The essential features of the original structure are confirmed. Cadmium-oxygen distances (from water molecules) have values of 2.26 and 2.33 Å, and cadmium-oxygen distances (from nitrate groups) are 2.44 and 2.59 Å. The structure consists of tetra-aquocadmium nitrate groups joined by hydrogen bonds.

Introduction

This structure was first solved from Patterson and electron density projections (Matković & Ribar, 1963). The results obtained may be summarized as follows: The cadmium-oxygen (water) distances are smaller than cadmium-oxygen (nitrate group) distances and the compound was described as tetra-aquocadmium nitrate. Two of the three oxygen atoms from the nitrate group are much closer to the cadmium atom than the

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third one. The range of bond distances between cadmium and eight oxygen atoms (four from water molecules and four from nitrate groups) located around the cadmium atom was only about 0.3 Å; hence, the cadmium atom is assigned the coordination number eight.

In the previous work precise coordinates of all the atoms except cadmium, which lies in the special position, could not be derived from electron density projection because of overlapping of the maxima. From these data it was not possible to obtain accurate bond distances or to determine with certainty the shape of the molecule. The present paper describes the structure derived from a three-dimensional anisotropic refinement.

Experimental

Single crystals of cadmium nitrate tetrahydrate were obtained by slow evaporation of an aqueous solution. The crystals are orthorhombic, space group $Fdd2(C_{2n}^{19})$, with unit-cell dimensions

$$a = 5.828 \pm 0.005 \text{ Å}$$

$$b = 25.86 \pm 0.03$$

$$c = 11.002 \pm 0.005$$

$$D_m = 2.46 \text{ g.cm}^{-3}$$

$$D_x = 2.47 \text{ g.cm}^{-3}$$

$$Z = 8$$

The unit-cell dimensions were obtained from a powder diffractometer pattern calibrated with germanium lines. The uncertainties in the cell dimensions given above correspond to estimated maximum errors. The density was determined pycnometrically.

Specimens chosen for collecting the intensity data were sealed in Lindemann glass capillary tubes because the compound is not stable in air. The three-dimen-

sional intensity data were recorded from crystals on multiple equi-inclination Weissenberg photographs, with Cu $K\alpha$ radiation. A crystal was ground to a sphere of 0.19 mm radius ($\mu = 227.21 \text{ cm}^{-1}$, $\mu r = 4.2$) in order to apply absorption corrections more easily and accurately. Such a ground specimen, mounted along the a axis, was used for collecting 0kl to 5kl intensity data. The maximum possible value of h index was 7 for Cu $K\alpha$ radiation, but on account of the limitation of the camera design, reflections up to the fifth laver only could be recorded in the a-axis setting. Crystals mounted along b and c axes were used to collect almost all other reflections lying within the Cu $K\alpha$ sphere. For this purpose one cylindrical specimen with a radius of 0.087 mm ($\mu r = 2.0$) oriented along [001] was used for collecting hk0 to hk4 reflections and another cylindrical specimen with a radius of 0.29 mm ($\mu r = 6.6$) oriented along [010] was used for collecting h0l to h4l reflections. The relative intensities were determined from the optical densities of each spot measured by means of a microdensitometer. The corrections for absorption. polarization and Lorentz factors were made in the usual way and the structure amplitude derived. The factors for translating the observed structure amplitude into the absolute scale were found for reflections of each layer and with the help of these factors, all structure amplitudes were scaled. The three-dimensional Fourier syntheses were computed on the ZUSE Z23 computer using the phase-angles as they were derived from the parameters of all the atoms resulting from the two-dimensional data. The calculation was carried out in the Institute Boris Kidrič, Vinča, Yugoslavia. The program was made by Zelenko & Zakrajšek (1964). The three-dimensional Fourier map confirmed the original structure.

Table 1. Fractional coordinates for cadmium nitrate tetrahydrate The thermal parameters are of the form $T = \exp \left[-(\beta_{11}h^2 + \beta_{22}k^2 + \beta_{33}l^2 + 2\beta_{12}hk + 2\beta_{13}hl + 2\beta_{23}kl) \right]$. Each thermal parameter is multiplied by 10⁴. Standard errors are given in parentheses.

	x	У	z	β_{11}	β22	β_{33}	β_{12}	β_{13}	β_{23}
Cd(1.00)	0.0	0.0	0.0	191 (5)	8 (0·2)	38 (1)	-3 (2)	are req to be by sym	uired zero metry
O(2·00)	0·3412	0·0469	-0.0645	215	5	100	5	8	2
	(0·0028)	(0·0005)	(0.0021)	(44)	(2)	(17)	(8)	(26)	(5)
O(3·00)	0·1427	0·0923	0·0524	292	18	157	- 8	64	- 3
	(0·0042)	(0·0009)	(0·0032)	(70)	(4)	(29)	(13)	(42)	(10)
O(4·00)	0·4650	0·1225	0·0096	316	12	109	- 10	148	9
	(0·0031)	(0·0006)	(0·0035)	(76)	(2)	(23)	(9)	(45)	(10)
O(5·00)	0·2512	-0.0244	0·1456	378	15	104	20	- 54	0
	(0·0038)	(0.0008)	(0·0023)	(70)	(3)	(20)	(14)	(44)	(7)
O(6·00)	0·1825	-0.0498	-0.1480	266	13	83	-2	-29	-4
	(0·0035)	(0.0007)	(0.0021)	(58)	(3)	(18)	(10)	(29)	(6)
N(7·00)	0·3198	0·0875	-0.0105	233	14	48	- 5	-29	11
	(0·0038)	(0·0007)	(0.0021)	(53)	(3)	(15)	(10)	(28)	(6)

 $\begin{array}{l} R_1 = \sum_{hkl} ||F_o| - |F_c|| / \sum_{hkl} |F_o| = 0.084 \text{ (including unobserved reflections)} \\ R_2 = \sum_{hkl} ||F_o| - |F_c|| / \sum_{hkl} |F_o| = 0.070 \text{ (omitting unobserved reflections)} \\ R_3 = \sum_{hkl} ||F_o| - |F_c||^2 / \sum_{hkl} ||F_o|^2 = 0.090 \text{ (including unobserved reflections)} \end{array}$

Table 2. Observed and calculated structure factors

Within each group, the numbers, reading from left to right are l, $10F_o$, $10F_c$, 10A and 10B. A minus sign before $10F_o$ indicates an unobserved reflection. The numerical value is the estimated minimum observable value.

	H= 1 K=15	H= 2 ==22	H. 6 K. 6	H. 6 F. 0
4 3676 3201 3201 -39 8 2462 2227 2227 40 12 1641 1265 1264 24	L 1537 1558 1136 ICe5 3 1459 1463 872 -1175 5 606 593 408 430 7 998 IC38 499 -911 4 1156 ICE 78 785	0 1060 1065 1065 -C 2 -128 164 -1C2 -129 4 1043 1017 1C17 -37 6 -128 100 -77 63 8 942 872 871 132	0 2023 1956 1956 -C 2 635 613 -195 561 4 1401 174 1374 -33 6 -126 235 -232 38 8 136 129 139 -37	2 1379 1246 1260 -225 6 802 77# 770 115 H=6 kr 2
H# C K# 2 2 3691 4436 4425 -322 6 2874 2895 2881 -276 10 1163 1147 1146 49	11 639 643 428 -479 H# 1 K+17 1 897 906 736 -529	H+ 2 K=24 0 -128 227 227 C 2 1231 1152 1129 225	10 - 128 - 55 - 54 - 4 H+ 4 K+ 6 0 929 815 - 815 - 6	0 1138 1222 1222 -C 2 -126 211 2C9 27 4 981 930 930 -21 6 -128 228 205 1C1 8 587 650 643 -SC
14 779 945 544 -35 += 0 x+ 4 C 2275 2826 2826 -0	3 1010 1014 876 511 5 1436 1365 844 -1072 7 1167 1045 676 767 9 718 657 357 -551 11 527 623 469 411	4 -128 140 -28 -137 6 1055 1C38 1C37 54 8 -128 68 42 -54 H= 2 x=26	2 1760 1915 1901 226 4 -128 115 65 95 6 1497 1350 1350 2 8 -128 102 -13 101 1C 675 793 792 -25	2 858 512 887 -215
4 1788 1335 882 -1662 8 1737 1617 1617 -2 12 1073 994 964 21 ₩= 0 K= 6	F= 1 K=19 1 1369 1427 1243 700 3 1301 1213 1054 -600 5 1031 1044 433 ===	0 1346 1182 1182 -C 2 427 378 243 -290 4 917 929 929 17 6 -128 132 84 -1C2	M1 4 K1 8 0 2128 2169 2165 -C 2 -128 229 117 197 4 1600 1657 1618 -67	4 256 116 43 166 6 736 726 723 -55 8 -128 53 56 -15 24 6 Kr 6
2 1622 1509 1401 563 6 1507 2144 2114 -354 10 1392 1302 1293 157	7 1022 991 690 -711 9 763 804 593 544 11 516 578 426 -351	H+2 K+28 0 304 310 310 -C 2 842 854 853 -5C 4 -128 115 18 -115	6 1200 1242 1238 -31 6 128 213 103 -61 8 102 1097 1699 137 10 -128 191 189 -25 14 4 8410	C 669 655 655 -C 2 -128 202 -195 -57 4 864 829 824 6 Ha 6 Kc 8
0 2284 2608 2608 -0 4 3219 3331 3319 279 8 2074 2052 2008 429 12 1111 1048 1046 -56	1 1211 1286 1672 -716 3 1077 1035 649 763 5 1057 1054 922 -510 7 953 896 647 620	6 666 759 757 -43 H= 2 K=30 0 868 901 901 -C	C 313 278 278 C 2 1712 1557 1533 -27C 4 -128 332 328 -51 6 1245 1208 12C2 -119	0 -128 115 -115 C 2 770 851 835 161 4 -128 94 -43 -11
F≠ 0 K≥10 2 3269 3778 3419 1608 6 2273 2254 2250 141 10 1254 1602 1596 - 153	9 763 751 555 -505 H= 1 K=23 1 763 718 440 566 4 819 814 548 -546	2 -128 52 40 -33 4 540 657 656 -31 H= 3 K= 1 1 1556 1606 523 1312	8 ~128 308 298 -75 10 755 841 840 43 +* 4 X*12 0 1268 101 1101 -c	F= 6 K=10 C E34 772 772 -r 2 -128 53 51 -11 4 967 554 946 117
H= 0 K+12 0 1554 1507 1507 -C 4 2656 2714 2690 388	5 875 876 573 662 7 752 764 608 -463 9 382 478 377 244 M+ 1 K+25	3 1818 2C21 537 -1791 5 1373 1457 1388 444 7 1050 1C09 430 -913 9 1050 973 664 711 11 875 785 5C5 -601	2 -128 56 47 -146 4 1281 1206 1168 -301 6 -128 23 -17 -15 8 1102 608 900 -122 10 -128 5 -64 -13	H= 6 K=12 0 -128 Y3 73 C 2 77C 855 844 16C 4 -124 121 118 -26
8 1596 1581 1580 -63 12 996 556 921 -256 H# C K=14	1 797 796 375 -702 3 774 716 328 636 5 527 461 318 -334 7 606 605 472 375	▶= 3 K# 3 1 2095 2072 1228 -1668 3 1737 1876 1340 1313 5 1376 1360 1340 1313	H+ 4 K+14 0 -128 187 187 (2 1399 1408 1401 -140 139 1408 1401 -17	H= 6 K=14 C 7C4 712 717 -0 2 -128 93 68 30
6 1099 1668 1666 70 10 1379 1241 1235 -127 12 0 K+16	⊷ 1 K+27 1 718 734 356 642 3 684 658 378 -538 5 897 897 663 663	7 1023 904 505 785 5 1037 955 805 -514 11 741 655 471 511 H# 3 K1 5	6 1066 561 960 45 8 -128 226 -217 -34 16 517 769 769 -3 H= 4 K=10	H 6 K = 16 J = 128 14 14 (2 533 631 630 21
C 1685 1693 1693 -0 4 2044 2002 20C2 27 8 1482 1367 1366 -59 12 626 788 774 143	7 494 535 410 -344 H= 1 K=29 1 #31 775 520 -580	1 1548 1819 1098 1451 3 1656 1767 1653 -627 5 1319 1259 793 977 7 1104 964 797 -543	0 1390 1406 1406 -C 2 -128 215 17 -214 4 1401 1375 1357 224 6 -128 73 -47 64	4 - 128 93 ×1 - 47 2* 6 ×=18 0 643 763 763 -C
++ 0 ++18 2 1941 1936 176C -793 6 1290 1314 1306 148 10 919 90C 896 83	3 763 829 642 524 5 415 462 333 - 320 H+ L x+31	9 822 742 530 518 11 700 654 575 -312 H= 3 K= 7	8 815 818 817 >0 >++ 4 K+[2 0 521 475 473 -C 2 1245 1276 1275 -16	2 -128 74 72 -31 ++ 7 K 1 1 391 482 258 407 1 397 491 145 -345
H# C K+2C 0 1462 1947 1947 -c 4 1303 1299 1259 - 8 945 843 863 -184	3 555 544 425 -339 ⊬# 2 KI 0 2 2870 3121 3121 49	3 1155 957 853 516 5 1064 555 901 -3C3 7 1211 1269 681 823 9 875 817 6C1 -553 11 633 572 442 363	4 -128 162 115 -114 6 1030 965 660 102 8 -128 147 146 -15 N# 4 K+20	HE 7 KE 3 1 456 489 285 -357 3 457 489 213 440
F= 0 X=22 2 1840 1948 1041 -503 6 1022 1081 1077 88	6 2176 1527 1883 466 10 1719 1554 1551 47 H#.2 K# 2	►= 3 K= 4 1 969 952 590 747 3 969 876 729 -4€1	0 70% 65% 658 C 2 -128 196 179 -8C 4 1138 981 680 45 6 -128 202 152 -132 8 -128 724 733 -133	F4 7 K= 5 1 344 343 275 28(3 369 405 240 -305
13 884 721 780 21	2 1281 1210 427 -113 4 2777 3101 3C91 257 6 779 664 518 -417 8 1595 1562 1562 -21 1C -128 154 136 -72	7 1333 1256 647 -1076 9 868 813 652 486 11 606 601 371 -473	0 -128 61 -61 C 2 815 751 751 -27	H# 7 K= 7 1 466 513 377 -34F 3 524 45H 35U 241
8 945 883 878 -87 += 0 K+26 2 1099 1167 1158 -140	12 58C 943 943 22 F= 2 K+ 4 C 1294 1190 1190 -0	1 1495 1605 839 -1366 3 1131 1644 755 722 5 1360 1250 581 -774 7 1535 1427 909 1100	4 - 128 54 17 - 51 6 767 738 737 37 744 6 8 24	HE T KE 9 1 364 494 371 326 3 369 449 314 -321
6 881 881 877 -83 ←= C K+28 0 461 485 485 -C	4 2249 2528 2500 - 376 4 830 780 - 156 - 764 6 1583 1604 1604 21 8 - 128 305 166 - 286 10 1470 1401 1390 - 175 12 - 128 105 84 61	9 1172 994 594 -796 11 660 703 506 487 H= 3 x=13 1 1104 1136 829 777	2 -128 205 -51 144 4 910 857 847 134 6 -128 40 -39 24	1 385 535 360 -855
2 639 71C 673 223	H= 2 K= 6 0 2753 2993 2993 -C 2 879 786 114 -778	3 1481 1381 1170 -734 5 1548 1415 961 1035 7 1387 1276 938 -876 9 801 789 556 438 11 538 569 446 -353	0 - 128 128 - 128 C 2 839 H03 8C3 - 3 4 - 128 116 88 75	
н+ С К+32 0 651 653 653 -0 н=1 к=1	4 2526 2713 2704 221 6 -128 285 -259 114 8 1646 1618 1604 -215 10 -128 304 -296 67 12 1043 1005 1605 1	≻+ 3 X+15 1 1373 1273 1616 -767 3 875 847 656 536	,= 4 ×+28 ∪ 659 696 646 -C ++ 5 ×+ 1	
1 2008 2071 878 -187 3 1963 1818 105 181 5 1671 1473 1245 -78 7 1425 1414 - 979 1022 9 1072 1007 591 -816	++ 2 K+ 8 0 1086 1005 1009 C 2 2840 3253 3207 -547 4 -128 441 -359 257	7 868 699 544 435 9 768 699 544 435 11 499 544 467 274 H# 3 8417	1 840 781 534 -57C 3 675 654 507 421 5 719 773 544 -548 7 715 698 467 518 9 486 535 227 -485	
11 831 825 550 613 13 549 597 405 -434 += 1 K= 3	6 2111 2180 2167 239 8 -126 377 -559 116 10 1281 1236 1234 65 12 -128 144 -47 135	1 902 819 504 646 3 1050 936 715 -664 5 902 772 570 520 7 552 544 362 -407	H= 5 X+ 3 1 1224 1135 974 583 3 897 A67 7C3 -566	
1 2008 2003 1011 2013 3 2389 2662 552 -266 5 2210 7424 1262 207 7 1795 1757 1490 -93 9 1279 1237 819 92	C 2631 2814 2814 -C 2 -128 235 230 65 4 1671 1765 1768 -64 6 -128 128 -13 128	4 445 444 257 368 H4 3 K419 1 1050 1011 747 -682 1 1023 1045 743 742	5 903 797 403 688 7 934 785 501 -863 9 862 588 323 451 H4 5 8* 5	
11 406 838 304 -811 13 662 732 486 54 H+ 1 K+ 5 1 2266 2540 1643 -1931	à 1458 1394 1390 -95 10 -128 58 -11 57 12 866 875 ∧68 104 ∺+ 2 K+12	5 754 713 364 -613 7 687 572 286 455 9 565 507 409 -3CC H= 3 K+21	1 1042 1281 956 -505 3 997 1206 807 601 ⊁= 5 K= 7	
3 2681 2981 1350 265 5 1761 1764 1202 -131 7 1884 1866 1689 76 9 1447 1344 940 -96 11 976 964 626 73	0 843 595 -555 C 2 1458 1541 1451 - 351 4 - 128 272 228 -148 6 1483 1439 1433 - 13C 8 - 128 126 126 6	1 1091 1037 765 761 3 1158 1032 860 -793 5 942 856 757 395 7 660 571 439 -366	1 992 965 763 615 3 1097 1126 781 -811 5 5 K 9	
13 639 676 509 -44 H= 1 K= 7 1 2188 2354 2222 77 1 160 2459 345 -161	10 904 854 853 36 12 -128 97 76 -61 4+ 2 K+14	4 444 805 381 47C H+ 3 K+23 1 888 815 577 -576 3 1C23 402 786 441	3 768 788 457 642 H4 5 X411 1 780 777 443 666	
5 1452 2023 1847 82 7 1414 1274 1159 -52 4 1021 979 767 60 11 1032 938 615 -70 13 516 566 480 30	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	5 822 756 419 -630 7 538 537 472 257 H= 3 K=25	3 818 752 421 -623 H= 5 K=13 1 725 706 633 -314	
▶# 1 K⊂ 9 1 1750 1612 1590 -26 3 2165 228C 1568 165 5 1100 1340 817 -91	12 666 785 784 22 6 H= 2 K=16 5 0 608 597 -597 C	1 808 /58 554 51/ 3 673 637 362 -525 5 485 477 368 277 7 364 44C 305 -317 be 3 8427	3 711 737 878 884 ₩7 5 Kel5 1 890 847 766 467 3 608 632 449 -445	
7 1043 1013 950 35 9 931 902 673 -60 11 639 629 445 44 13 563 656 494 -42	j 2 2123 2250 2218 377 0 4 -128 394 322 147 5 6 1721 1698 1698 -34 2 8 -128 351 145 -35 2 8 -128 151 146 35 10 992 1018 1C16 62	1 565 550 379 -398 3 606 580 363 452 5 485 504 411 -252	H# 5 K#17 1 759 710 390 -594 3 658 697 442 535	
H= 1 K=11 1 2536 2763 2004 150 3 1907 2020 1325 -152 5 1021 1051 721 76 7 997 1041 481 -4	H= 2 K×18 3 5 0 1962 1923 1623 -C 5 2 -128 393 84 384 3 4 1620 1607 1604 -1C5	H= 3 X-29 1 * 512 54C 433 323 3 350 417 347 -231 H= 4 K= 0	H± 5 X*[9 1 678 665 389 54C 3 578 531 283 -45C	
9 1077 1018 559 85 11 819 800 589 -54 13 382 505 329 38	c 6 -128 160 68 144 1 8 1306 1233 1230 88 3 1C -128 102 79 -64 += 2 K+20	C 1841 1678 1678 -0 4 1665 1508 1507 43 8 1578 1410 1393 219	H= 5 K=21 1 607 542 360 -405 3 409 471 326 339 4 H=32	
1 1694 1743 1155 -130 3 1683 1787 1119 139 5 2064 2087 1331 -160 7 1100 1084 633 88 9 724 734 557 -47	6 0 -128 103 -103 C 3 2 1306 1215 1359 363 8 4 -128 209 -25 208 C 6 1181 114C 1123 -200 6 -128 53 -41 34	H= 4 X= 2 0 304 249 -249 C 2 1497 1501 1449 351 4 -128 231 150 176 6 1748 1615 1612 -95	++ > K=23 1 476 459 397 231 3 389 44€ 397 -185	
11 718 756 461 59	ç 10 691 771 766 -81	8 -128 110 13 165 10 791 991 531 18 12 -128 8 4 -7		

Refinement of the structure

The coordinates of the atoms obtained from two-dimensional data were subjected to a least-squares refinement by the ORFLS program of Busing, Martin & Levy (1962). Four cycles of weighted least-squares refinement with isotropic and two cycles with anisotropic temperature factors were performed. A modified version of the Hughes weighting scheme (Hughes, 1941) was used; the standard deviation for each reflection was computed by the equations

$$\sigma = |F_o|/4|F_{\min}| \text{ for } |F_o| > 4|F_{\min}|$$

$$\sigma = 4|F_{\min}|/|F_o| \text{ for } |F_o| \le 4|F_{\min}|$$

Structure factors for unobserved reflections were assigned one-half the minimum observed |F| and were omitted from the refinement if the calculated structure factor was less than the minimum observed structure factor. After the last cycle of refinement the shifts in the atomic coordinates were less than standard deviations. In the course of this refinement the *R* index decreased to 0.084. The refined atomic coordinates and temperature factors are listed in Table 1. The observed and calculated structure factors are listed in Table 2. The atomic scattering factors used in these calculations were from *International Tables for X-ray Crystallo*graphy (1962). No dispersion correction for cadmium atomic scattering factors was applied. Bond distances and angles were computed with the Busing, Martin & Levy (1964) ORFFE, Fortran function and error program.

The refinement cycles and the calculation of bond lengths were carried out on the IBM 709 computer at Washington State University, where one of the authors (B.M.) has a postdoctoral fellowship.

Description and discussion of the structure

The numbering of the atoms, which is the same in all Figures and Tables, is listed in Table 3. The bond distances in the cadmium nitrate tetrahydrate group are listed in Table 4. Fig. 1 represents the projection of the structure on the xy plane, and Fig. 2 a view down one cadmium nitrate tetrahydrate group. There are two short cadmium-oxygen (water) distances, 2.26 and 2.33 Å, and two longer cadmium-oxygen (nitrate group) distances, 2.44 and 2.59 Å. The shorter cadmium-oxygen distances are indicated in Fig. 2 by broken lines, and



Fig. 1. Projection of the structure of cadmium nitrate tetrahydrate on a plane normal to [001]. Big open circles are cadmium atoms, medium open circles are nitrate-oxygen atoms, shaded medium circles are water molecules, and small shaded circles are nitrogen atoms. Only these atoms are numbered whose distances are mentioned in tables.

the nitrate-oxygen distances by full lines. The third oxygen atom of the nitrate group, O(4.00), is over 4 Å from the cadmium atom, and hence not listed in Table 4. The distances from the cadmium atom to the eight nearest oxygen atoms range from 2.26 to 2.59 Å, and it appears reasonable to assign cadmium a coordination

number eight. Such a polyhedron is shown in Fig. 3, which represents the same view down the cadmium nitrate tetrahydrate group as in Fig. 2. The cadmium atom lies on the twofold axis inside the oxygen polyhedron and it is omitted from this figure. The oxygen polyhedron has eight vertices, four of which are nitrate oxygen atoms

	Table 3. Numbe	ering of the a	toms*
The atoms	in the asymmetric	unit and their	closest neighbors

. .

The coordinates of atoms

-

In asymmetric unit		Transfo	ormed by s	ymmetry		Trar	isformed by	symmetry an	d translated	by cell
x, y, z.	-x, -y, z.	$\frac{\frac{1}{4}-x}{\frac{1}{4}+y},$ $\frac{1}{4}+z.$	$\frac{\frac{1}{4} + x}{\frac{1}{4} - y},$ $\frac{1}{4} + z.$	$\frac{\frac{1}{2}-x}{-y},\\ \frac{1}{2}+z.$	$1-x, \\ -y, \\ z.$	$\overline{\frac{\frac{3}{4}-x}{\frac{3}{4}+y-1}},$ $\frac{\frac{1}{4}+z}{\frac{1}{4}+z}.$	$\frac{\frac{1}{2}-x}{-y},$ $\frac{1}{2}+z-1.$	$\frac{3}{4} - x,$ $\frac{1}{4} + y,$ $\frac{3}{4} + z - 1.$	$\frac{3}{4} + x - 1,$ $\frac{1}{4} - y,$ $\frac{3}{4} + z - 1.$	$\frac{1}{4} - x,$ $\frac{3}{4} + y - 1,$ $\frac{3}{4} + z - 1.$
Cd(1.00) O(2.00) O(3.00) O(4.00) O(5.00)	O(2·01) O(3·01) O(4·01)		O(2·03) O(3·03) O(4·03)	O(2·06)	O(2·11) O(4·11)	O(4·24)	-		O(4·58)	O(3·69) O(4·69)
O(5.00) O(6.00) N(7.00)	O(5.01) O(6.01) N(7.01)	O(6·02)	N(7·03)	O(5·06) O(6·06)	O(5·11) O(6·11)		O(5·46)	O(5·47)		

* Atoms are designated by a three place number which identifies the atom, the cell translation and the symmetry transformation. Only those atoms are numbered whose distances and angles are mentioned in tables.

Table 4. Interatomic distances and bond angles in cadmium nitrate tetrahydrate group

Standard errors are given in parenthesis.

Cd-OH ₂ distances Cd($1\cdot00$)-O($5\cdot00$) Cd($1\cdot00$) O($6\cdot00$)	2·26 (0·02) Å	$O-OH_2$ distances $O(2\cdot00)-O(6\cdot00)$	2·82 (0·02) Å
Cu(100) = O(000)	2.33 (0.02)	O(2.00) = O(5.00)	3.00 (0.03)
		O(3.00) = O(3.01)	3.07(0.03)
		O(3.00) = O(0.01)	3.10(0.04)
Cd-O (from NO ₂) dist	ances	O(2.00) = O(0.01) O(3.00) = O(5.00)	3.16(0.03)
Cd(1.00) = O(2.00)	2.44 (0.02) Å	0(3.00)-0(3.00)	3.23 (0.03)
Cd(1.00) = O(3.00)	2.59(0.02)		
24(100)-0(500)	2 59 (0 02)	H.O. OH. distances	
		$\Omega(5.00) \Omega(5.01)$	2.10 (0.04) \$
		O(5.00) = O(5.01)	3.19 (0.04) A
Cd–N distance		O(6.00) = O(6.01)	3.32(0.03)
Cd(1.00) = N(7.00)	2·93 (0·02) Å	0(000)-0(001)	5.24 (0.04)
	2 33 (0 02) 11	O-N-O angles in NO ₂ group	•
O-N distances in NO ₂	group	O(2.00) = N(7.00) = O(3.00)	116.49(2.19)
O(2.00) - N(7.00)	1.21(0.03) Å	O(2.00) - N(7.00) - O(3.00)	120.7(2.1)
O(3.00) - N(7.00)	1.25 (0.03)	O(3.00) = N(7.00) = O(4.00)	1297(23) 112.7(2.1)
O(4.00) - N(7.00)	1.26 (0.03)	0(5 00)=11(7 00)=0(4 00)	1127(2.1)
	- == (0 00)	O-Cd-O angles in Cd polyh	edron
H ₂ O–N distances		O(2.00) = Cd(1.00) = O(3.00)	48.9°(0.7°)
O(5.00) - N(7.00)	3·39 (0·02) Å	O(6:00) = Cd(1:00) = O(2:00)	72.5 (0.6)
O(6.00)-N(7.00)	3.94 (0.03)	O(6.00) = Cd(1.00) = O(3.01)	77.9 (0.9)
		O(5:00) - Cd(1:00) - O(3:01)	78.1(0.9)
O-O distances between	NO ₃ oxygens	O(5.00) - Cd(1.00) - O(2.00)	79.5 (0.8)
O(2·00)–O(3·00)	2.09 (0.03) Å	O(6.00) - Cd(1.00) - O(2.01)	83.8 (0.7)
O(3·00)-O(4·00)	2.09 (0.03)	O(5.00) - Cd(1.00) - O(3.00)	83.9 (0.9)
O(2·00)–O(4·00)	2.24 (0.03)	O(5.00) - Cd(1.00) - O(5.01)	89.8 (1.2)*
	. ,	O(6.00) - Cd(1.00) - O(6.01)	91.5 (1.1)*
		O(5.00) - Cd(1.00) - O(6.00)	92.6 (0.8)
		O(6.00) - Cd(1.00) - O(3.00)	121.1 (0.8)
		O(5.00) - Cd(1.00) - O(2.01)	126.6 (0.7)
		O(2.01) - Cd(1.00) - O(3.00)	141.8 (0.7)
		O(2.00) - Cd(1.00) - O(2.01)	146.0 (1.1)*
		O(3.00) - Cd(1.00) - O(3.01)	154.6 (1.6)*
		O(5·00)–Cd(1·00)–O(6·01)	160•7 (0•7)

* All values of O-Cd-O angles, except those designated by asterisks, appear twice in the polyhedron.

[O(2.00), O(2.01), O(3.00) and O(3.01)] and four oxygen from water molecules [O(5.00), O(5.01), O(6.00) and O(6.01)]. The oxygen atoms which belong to this distorted polyhedron are connected in Fig. 3 with full lines and dotted lines, and the twofold axis is indicated by a full and broken line. The oxygen edges of the polyhedron vary in length over a fairly narrow range from 2.82 to 3.34 Å, apart from two much shorter edges (2.09 Å), which are sides of the NO₃ triangle adjoining the cadmium polyhedron [the distances between the atoms O(2.00)–O(3.00) and O(2.01)–O(3.01)]. The polyhedron around Cd may be described as a distorted dodecahedron. The distances between oxygen atoms which belong to this polyhedron and angles around Cd atom are listed in Table 4. For comparison,



the regular dodecahedron has 4 longer and 14 shorter edges and 28 angles, which are as follows: $74^{\circ}24'(14)$, $98^{\circ}44'(4)$, $130^{\circ}12'(4)$, $136^{\circ}48'(2)$, $148^{\circ}48'(4)$.

Intermolecular distances between atoms of the asymmetric unit and their nearest neighbors are listed in Table 5 and illustrated in Fig. 1. They require no special comment. Some $O \cdots O$ contacts between the atoms



Fig. 3. A view down the polyhedron of oxygen atoms around the cadmium atom, which is omitted in the figure. It lies in the center of the molecule and a twofold axis is passing through it dividing the O(5.00)-O(5.01) and O(6.00)-O(6.01)distances. Open circles are nitrate-oxygen atoms, shaded circles are water molecules, and small shaded circles are nitrogen atoms.

Fig. 2. A view down the cadmium nitrate tetrahydrate group. Big open circle is cadmium atom, medium open circles are nitrate-oxygen atoms, shaded medium circles are water molecules, and small shaded circles are nitrogen atoms.

Table 5. Intermolecular distances less than 3.40 Å between the neighboring atoms of the asymmetric unit

Standard errors are given in parenthesis.

O-O distances		O-OH ₂ distances	
O(4·00)–O(2·03) O(2·00)–O(4·58)	2·93 (0·04) Å	O(3·00)–O(6·02) O(6·00)–O(3·69)	2·87 (0·03) Å
O(2·00)-O(2·11)	3.06 (0.03)	O(2.00) - O(6.11) O(6.00) - O(2.11)	2.93 (0.03)
O(4·00)–O(4·03) O(4·00)–O(4·58)	3.12 (0.02)	O(4.00) - O(5.47) O(5.00) - O(4.24)	2.96 (0.03)
O(4·00)–O(3·03) O(3·00)–O(4·58)	3·36 (0·05)	O(4.00) - O(6.02) O(6.00) - O(4.69)	3.23 (0.03)
O-N distances	2.70 (0.04) \$	O(2·00)-O(5·46) O(5·00)-O(2·06)	3.29 (0.03)
N(7.00) - N(7.03) N(7.00) - O(4.58)	2·79 (0·04) A	O(6·00)-O(4·11) O(4·00)-O(6·11)	3.28 (0.03)
H_2O-OH_2 distances	2.00.(0.02) Å	O(2·00)–O(5·11) O(5·00)–O(2·11)	3.37 (0.03)
O(5.00)-O(5.46) O(5.00)-O(5.11)	3·16 (0·05) A	O(4·00)–O(5·11) O(5·00)–O(4·11)	3.37 (0.04)

of neighboring molecules have a range of values increasing from 2.87 Å. These distances between nitrateoxygen and water-oxygen atoms or between wateroxygen atoms indicate possible hydrogen bonding between the atoms of neighboring cadmium nitrate tetrahydrate groups. Further evidence is provided by the list of angles around water molecules also given in Table 6. These angles, selected because their values were close to the HOH bond angle in H₂O, may be used in conjunction with the distances to select possible hydrogen bond locations. Based on the distances and angles hydrogen bonds are probably between O(4.24)-O(5.00)-O(6.06) and O(3.69)-O(6.00)-O(2.11)atoms.

Table 6. Selected angles involving water oxygen atoms

O(5·11)-O(5·00)-O(2·06)	102·8° (0·5°)
O(4·24)-O(5·00)-O(6·06)	104.1 (1.1)
O(4.24) - O(5.00) - O(6.00)	104.2 (1.0)
O(3.69) - O(6.00) - O(2.11)	103.2 (0.9)
O(5.46) - O(6.00) - O(4.69)	104.8 (1.0)
O(4·69)-O(6·00)-O(4·11)	105.0 (0.6)

The values of the intermolecular distances obtained during this refinement are not significantly different from the results obtained before. The cadmium-oxygen distances, obtained after refinement, are a little shorter than reported previously. The shortest one is 2.26 Å. This length is 0.09 Å shorter than the cadmium-oxygen distance in CdO which has a sodium chloride structure (Wyckoff, 1963). The values of two shorter cadmiumoxygen distances (2.26 and 2.33 Å) are also in good agreement with those already found in other cadmium compounds; e.g. the cadmium-oxygen distance in monomethylureacadmium chloride is 2.18 Å, in bisacetamide-cadmium chloride is 2.23 Å, in bisthiourea-cadmium formate is 2.28 Å, in bisurea-cadmium chloride is 2.28 Å and in bisbiuret-cadmium chloride is 2.34 Å (Nardelli, Fava-Gasparri & Boldrini, 1965). A still

shorter cadmium-oxygen (water) distance of 2.12 Å was found in the structure of tricadmium sulphate octahydrate (Lipson, 1936). For comparison, in this structure the distances of six nearest atoms (four sulphate oxygen atoms and two from water molecules) located around the cadmium atom vary from 2.12 to 2.63 Å. In the structure of cadmium nitrate tetrahydrate the distances of eight nearest atoms (four from water molecules and four nitrate oxygens) around the cadmium atom range from 2.26 to 2.59 Å. The distances in the NO₃ group do not deviate significantly from the results obtained before and are in agreement with the known data (International Tables for X-ray Crystallography, 1962). The O-N-O angles in the NO₃ groups indicate that the nitrogen atom lies in the plane of the oxygen triangle within the error of experiment.

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