

respectively 0.024 Å and -0.060 Å out of this plane; this is partly because the carboxylic group makes a small angle of 3.3° with the benzene ring plane and may partly be due to the fact that the oxygen atoms are drawn towards the centre of the dimer, presumably because of the force exerted by the hydrogen bonds. This is indicated by the unequal distances of the two oxygen atoms from the benzene ring plane and by the fact that the distance of the centre of the dimer from the plane of the carboxylic group (-0.047 Å) is less than its distance from the benzene ring plane (-0.118 Å).

The observed value of 1.501 Å for the exocyclic C-C bond length is the expected single bond distance between the carbon atoms in  $sp^2$  states of hybridization. This indicates that there is no appreciable degree of conjugation across this bond; this fact again suggests that as expected, there is no contribution from quinonoid valence bond structure in *p*-nitrobenzoic acid.

The nitrogen atom N is -0.047 Å out of the plane of the benzene ring. The atom C(4) is 0.121 Å away from the plane of the nitro group; the angle between this and the benzene ring plane is 13.7°. The C-N bond length of 1.480 Å is significantly longer than the corresponding bond lengths in *p*-nitroaniline (1.460 Å),  $\alpha$ -*p*-nitrophenol (1.442 Å) and  $\beta$ -*p*-nitrophenol (1.450 Å). The mean of the two N-O bond lengths in *p*-nitrobenzoic acid is 1.216 Å. In *p*-nitroaniline and  $\beta$ -*p*-nitrophenol, the corresponding lengths after correction for thermal motion are 1.247 Å and 1.242 Å respectively. There is pronounced torsional oscillation of the nitro group in these latter structures and the correction for torsional effects in N-O distances is about 0.018 Å. In the present study, anisotropic thermal parameters have not been obtained; however, the individual isotropic temperature factors for the oxygen atoms of the nitro group (Table 1) are not much larger than the values

for other atoms; there is thus no suggestion of pronounced torsional oscillation of the nitro group. It thus appears that the N-O bonds in *p*-nitrobenzoic acid are significantly shorter than those in *p*-nitroaniline and *p*-nitrophenol. The shortening of the N-O bonds and the elongation of the C-N bond in *p*-nitrobenzoic acid from the corresponding values in *p*-nitroaniline and *p*-nitrophenol further supports the view that the bond length variations are due to minor contributions from quinonoid valence bond structures in the latter compounds.

The arrangement of molecules in the unit cell is shown in Fig. 2, in which the principal intermolecular distances are also shown.

We are grateful to Dr A. B. Biswas for his kind interest in this work.

#### References

- COCHRAN, W. (1948). *J. Sci. Instrum.* **25**, 253.  
 COPPENS, P. & SCHMIDT, G. M. J. (1965a). *Acta Cryst.* **18**, 62.  
 COPPENS, P. & SCHMIDT, G. M. J. (1965b). *Acta Cryst.* **18**, 654.  
 COX, E. G., CRUICKSHANK, D. W. J. & SMITH, J. A. S. (1958). *Proc. Roy. Soc. A*, **247**, 1.  
 DARLOW, S. F. (1960). *Acta Cryst.* **13**, 683.  
 LIPSON, H. & COCHRAN, W. (1953). *The Determination of Crystal Structures*, pp. 288, 309. London: Bell.  
 MOORE, F. H. (1963). *Acta Cryst.* **16**, 1169.  
 PHILLIPS, D. C. (1956). *Acta Cryst.* **9**, 819.  
 SAKORE, T. D. & PANT, L. M. (1965). *Indian J. Pure Appl. Phys.* **3**, 143.  
 SCHOMAKER, V., WASER, J., MARSH, R. E. & BERGMAN, G. (1959). *Acta Cryst.* **12**, 600.  
 TROTTER, J. (1960). *Tetrahedron*, **8**, 13.  
 TRUEBLOOD, K. N., GOLDISH, E. & DONOHUE, J. (1961). *Acta Cryst.* **14**, 1009.

*Acta Cryst.* (1966). **21**, 719

### Refinement of the Structure of $\text{Cd}(\text{NO}_3)_2 \cdot 4\text{H}_2\text{O}$

BY B. MATKOVIĆ, B. RIBAR\* AND B. ZELENKO  
*Institute Rudjer Bošković, Zagreb, Yugoslavia*

AND S. W. PETERSON  
*Washington State University, Pullman, Washington, U.S.A.*

(Received 29 September 1965 and in revised form 8 February 1966)

The crystal structure of  $\text{Cd}(\text{NO}_3)_2 \cdot 4\text{H}_2\text{O}$  has been refined by least-squares calculations to a final *R* index of 8.4%. The estimated standard deviations of atomic coordinates ranged from 0.0005 to 0.0042. The essential features of the original structure are confirmed. Cadmium-oxygen distances (from water molecules) have values of 2.26 and 2.33 Å, and cadmium-oxygen distances (from nitrate groups) are 2.44 and 2.59 Å. The structure consists of tetra-aquocadmium nitrate groups joined by hydrogen bonds.

#### Introduction

This structure was first solved from Patterson and electron density projections (Matković & Ribar, 1963). The

results obtained may be summarized as follows: The cadmium-oxygen (water) distances are smaller than cadmium-oxygen (nitrate group) distances and the compound was described as tetra-aquocadmium nitrate. Two of the three oxygen atoms from the nitrate group are much closer to the cadmium atom than the

\* Permanent address: Physics Department, Faculty of Science, The University, Sarajevo, Yugoslavia.

third one. The range of bond distances between cadmium and eight oxygen atoms (four from water molecules and four from nitrate groups) located around the cadmium atom was only about  $0.3 \text{ \AA}$ ; hence, the cadmium atom is assigned the coordination number eight.

In the previous work precise coordinates of all the atoms except cadmium, which lies in the special position, could not be derived from electron density projection because of overlapping of the maxima. From these data it was not possible to obtain accurate bond distances or to determine with certainty the shape of the molecule. The present paper describes the structure derived from a three-dimensional anisotropic refinement.

### Experimental

Single crystals of cadmium nitrate tetrahydrate were obtained by slow evaporation of an aqueous solution. The crystals are orthorhombic, space group  $Fdd2 (C_{2v}^9)$ , with unit-cell dimensions

$$\begin{aligned} a &= 5.828 \pm 0.005 \text{ \AA} \\ b &= 25.86 \pm 0.03 \\ c &= 11.002 \pm 0.005 \\ D_m &= 2.46 \text{ g.cm}^{-3} \\ D_x &= 2.47 \text{ g.cm}^{-3} \\ Z &= 8. \end{aligned}$$

The unit-cell dimensions were obtained from a powder diffractometer pattern calibrated with germanium lines. The uncertainties in the cell dimensions given above correspond to estimated maximum errors. The density was determined pycnometrically.

Specimens chosen for collecting the intensity data were sealed in Lindemann glass capillary tubes because the compound is not stable in air. The three-dimen-

sional intensity data were recorded from crystals on multiple equi-inclination Weissenberg photographs, with  $\text{Cu } K\alpha$  radiation. A crystal was ground to a sphere of  $0.19 \text{ mm}$  radius ( $\mu = 227.21 \text{ cm}^{-1}$ ,  $\mu_r = 4.2$ ) in order to apply absorption corrections more easily and accurately. Such a ground specimen, mounted along the  $a$  axis, was used for collecting  $0kl$  to  $5kl$  intensity data. The maximum possible value of  $h$  index was 7 for  $\text{Cu } K\alpha$  radiation, but on account of the limitation of the camera design, reflections up to the fifth layer only could be recorded in the  $a$ -axis setting. Crystals mounted along  $b$  and  $c$  axes were used to collect almost all other reflections lying within the  $\text{Cu } K\alpha$  sphere. For this purpose one cylindrical specimen with a radius of  $0.087 \text{ mm}$  ( $\mu_r = 2.0$ ) oriented along  $[001]$  was used for collecting  $hk0$  to  $hk4$  reflections and another cylindrical specimen with a radius of  $0.29 \text{ mm}$  ( $\mu_r = 6.6$ ) oriented along  $[010]$  was used for collecting  $h0l$  to  $h4l$  reflections. The relative intensities were determined from the optical densities of each spot measured by means of a microdensitometer. The corrections for absorption, polarization and Lorentz factors were made in the usual way and the structure amplitude derived. The factors for translating the observed structure amplitude into the absolute scale were found for reflections of each layer and with the help of these factors, all structure amplitudes were scaled. The three-dimensional Fourier syntheses were computed on the ZUSE Z23 computer using the phase-angles as they were derived from the parameters of all the atoms resulting from the two-dimensional data. The calculation was carried out in the Institute Boris Kidrič, Vinča, Yugoslavia. The program was made by Zelenko & Zakrajšek (1964). The three-dimensional Fourier map confirmed the original structure.

Table 1. Fractional coordinates for cadmium nitrate tetrahydrate

The thermal parameters are of the form  $T = \exp [-(\beta_{11}h^2 + \beta_{22}k^2 + \beta_{33}l^2 + 2\beta_{12}hk + 2\beta_{13}hl + 2\beta_{23}kl)]$ . Each thermal parameter is multiplied by  $10^4$ . Standard errors are given in parentheses.

	$x$	$y$	$z$	$\beta_{11}$	$\beta_{22}$	$\beta_{33}$	$\beta_{12}$	$\beta_{13}$	$\beta_{23}$
Cd(1·00)	0·0	0·0	0·0	191 (5)	8 (0·2)	38 (1)	-3 (2)	are required to be zero by symmetry	
O(2·00)	0·3412 (0·0028)	0·0469 (0·0005)	-0·0645 (0·0021)	215 (44)	5 (2)	100 (17)	5 (8)	8 (26)	2 (5)
O(3·00)	0·1427 (0·0042)	0·0923 (0·0009)	0·0524 (0·0032)	292 (70)	18 (4)	157 (29)	-8 (13)	64 (42)	-3 (10)
O(4·00)	0·4650 (0·0031)	0·1225 (0·0006)	0·0096 (0·0035)	316 (76)	12 (2)	109 (23)	-10 (9)	148 (45)	9 (10)
O(5·00)	0·2512 (0·0038)	-0·0244 (0·0008)	0·1456 (0·0023)	378 (70)	15 (3)	104 (20)	20 (14)	-54 (44)	0 (7)
O(6·00)	0·1825 (0·0035)	-0·0498 (0·0007)	-0·1480 (0·0021)	266 (58)	13 (3)	83 (18)	-2 (10)	-29 (29)	-4 (6)
N(7·00)	0·3198 (0·0038)	0·0875 (0·0007)	-0·0105 (0·0021)	233 (53)	14 (3)	48 (15)	-5 (10)	-29 (28)	11 (6)

$$R_1 = \frac{\sum_{hkl} |F_o| - |F_c|}{\sum_{hkl} |F_o|} = 0.084 \text{ (including unobserved reflections)}$$

$$R_2 = \frac{\sum_{hkl} |F_o| - |F_c|}{\sum_{hkl} |F_o|} = 0.070 \text{ (omitting unobserved reflections)}$$

$$R_3 = \frac{\sum_{hkl} w |F_o| - |F_c|}{\sum_{hkl} w |F_o|} = 0.090 \text{ (including unobserved reflections)}$$

Table 2. Observed and calculated structure factors

Within each group, the numbers, reading from left to right are I, 10F0, 10Fc, 10A and 10B. A minus sign before 10F0 indicates an unobserved reflection. The numerical value is the estimated minimum observable value.

Table with multiple columns of numerical data, organized into groups labeled with h, k, l indices (e.g., h=0 k=0, h=1 k=1, etc.). Each group contains several rows of values representing structure factors.

### Refinement of the structure

The coordinates of the atoms obtained from two-dimensional data were subjected to a least-squares refinement by the ORFLS program of Busing, Martin & Levy (1962). Four cycles of weighted least-squares refinement with isotropic and two cycles with anisotropic temperature factors were performed. A modified version of the Hughes weighting scheme (Hughes, 1941) was used; the standard deviation for each reflection was computed by the equations

$$\sigma = |F_o|/4|F_{\min}| \text{ for } |F_o| > 4|F_{\min}|$$

$$\sigma = 4|F_{\min}|/|F_o| \text{ for } |F_o| \leq 4|F_{\min}|$$

Structure factors for unobserved reflections were assigned one-half the minimum observed  $|F|$  and were omitted from the refinement if the calculated structure factor was less than the minimum observed structure factor. After the last cycle of refinement the shifts in the atomic coordinates were less than standard deviations. In the course of this refinement the  $R$  index decreased to 0.084. The refined atomic coordinates and temperature factors are listed in Table 1. The observed and calculated structure factors are listed in Table 2.

The atomic scattering factors used in these calculations were from *International Tables for X-ray Crystallography* (1962). No dispersion correction for cadmium atomic scattering factors was applied. Bond distances and angles were computed with the Busing, Martin & Levy (1964) ORFFE, Fortran function and error program.

The refinement cycles and the calculation of bond lengths were carried out on the IBM 709 computer at Washington State University, where one of the authors (B.M.) has a postdoctoral fellowship.

### Description and discussion of the structure

The numbering of the atoms, which is the same in all Figures and Tables, is listed in Table 3. The bond distances in the cadmium nitrate tetrahydrate group are listed in Table 4. Fig. 1 represents the projection of the structure on the  $xy$  plane, and Fig. 2 a view down one cadmium nitrate tetrahydrate group. There are two short cadmium-oxygen (water) distances, 2.26 and 2.33 Å, and two longer cadmium-oxygen (nitrate group) distances, 2.44 and 2.59 Å. The shorter cadmium-oxygen distances are indicated in Fig. 2 by broken lines, and

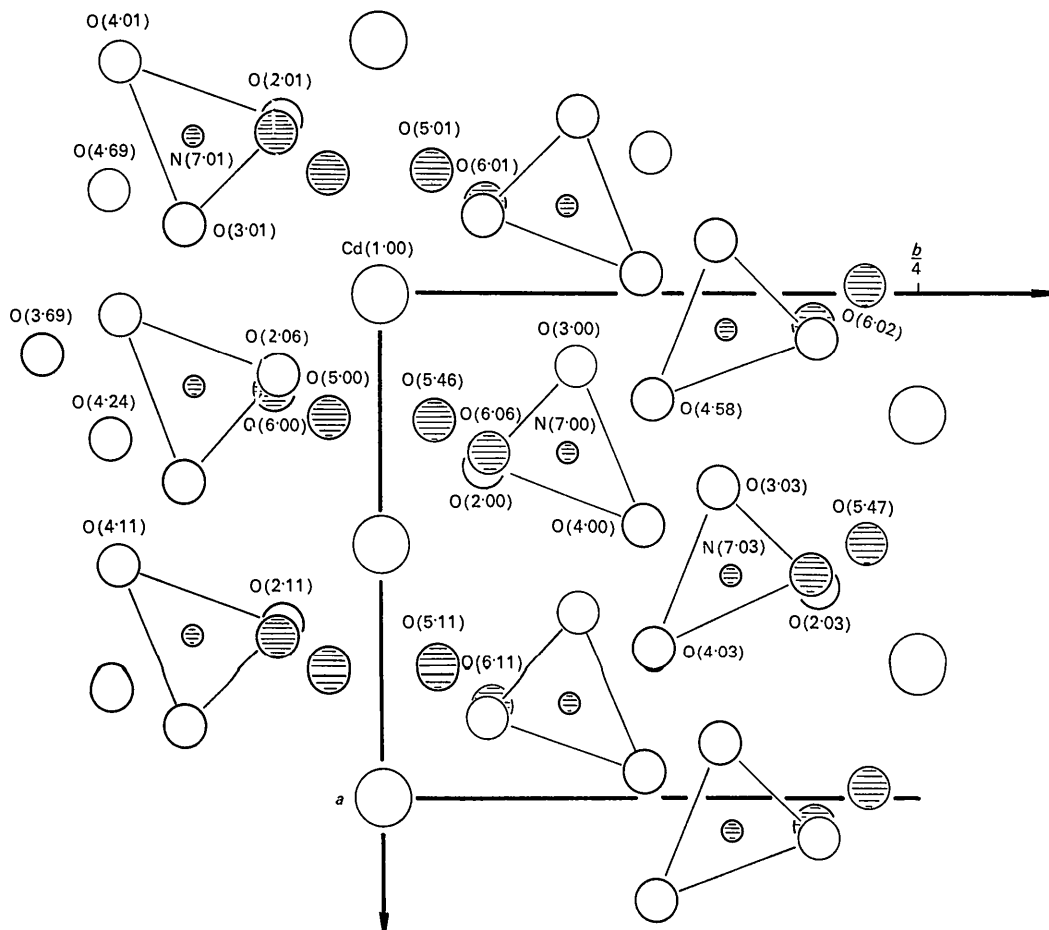


Fig. 1. Projection of the structure of cadmium nitrate tetrahydrate on a plane normal to  $[001]$ . Big open circles are cadmium atoms, medium open circles are nitrate-oxygen atoms, shaded medium circles are water molecules, and small shaded circles are nitrogen atoms. Only these atoms are numbered whose distances are mentioned in tables.

the nitrate-oxygen distances by full lines. The third oxygen atom of the nitrate group, O(4·00), is over 4 Å from the cadmium atom, and hence not listed in Table 4. The distances from the cadmium atom to the eight nearest oxygen atoms range from 2·26 to 2·59 Å, and it appears reasonable to assign cadmium a coordination

number eight. Such a polyhedron is shown in Fig. 3, which represents the same view down the cadmium nitrate tetrahydrate group as in Fig. 2. The cadmium atom lies on the twofold axis inside the oxygen polyhedron and it is omitted from this figure. The oxygen polyhedron has eight vertices, four of which are nitrate oxygen atoms

Table 3. *Numbering of the atoms\**

The atoms in the asymmetric unit and their closest neighbors

The coordinates of atoms

In asymmetric unit	Transformed by symmetry					Transformed by symmetry and translated by cell				
	$-x,$	$\frac{1}{2}-x,$	$\frac{1}{2}+x,$	$\frac{1}{2}-x,$	$1-x,$	$\frac{3}{2}-x,$	$\frac{1}{2}-x,$	$\frac{3}{2}-x,$	$\frac{3}{2}+x-1,$	$\frac{1}{2}-x,$
$x,$	$-x,$	$\frac{1}{2}-x,$	$\frac{1}{2}+x,$	$\frac{1}{2}-x,$	$1-x,$	$\frac{3}{2}-x,$	$\frac{1}{2}-x,$	$\frac{3}{2}-x,$	$\frac{3}{2}+x-1,$	$\frac{1}{2}-x,$
$y,$	$-y,$	$\frac{1}{2}+y,$	$\frac{1}{2}-y,$	$-y,$	$-y,$	$\frac{3}{2}+y-1,$	$-y,$	$\frac{1}{2}+y,$	$\frac{1}{2}-y,$	$\frac{3}{2}+y-1,$
$z,$	$z,$	$\frac{1}{2}+z,$	$\frac{1}{2}+z,$	$\frac{1}{2}+z,$	$z,$	$\frac{1}{2}+z,$	$\frac{1}{2}+z-1,$	$\frac{3}{2}+z-1,$	$\frac{3}{2}+z-1,$	$\frac{1}{2}+z-1,$
Cd(1·00)										
O(2·00)	O(2·01)		O(2·03)	O(2·06)	O(2·11)					
O(3·00)	O(3·01)		O(3·03)							O(3·69)
O(4·00)	O(4·01)		O(4·03)		O(4·11)	O(4·24)			O(4·58)	O(4·69)
O(5·00)	O(5·01)			O(5·06)	O(5·11)		O(5·46)	O(5·47)		
O(6·00)	O(6·01)	O(6·02)		O(6·06)	O(6·11)					
N(7·00)	N(7·01)		N(7·03)							

\* Atoms are designated by a three place number which identifies the atom, the cell translation and the symmetry transformation. Only those atoms are numbered whose distances and angles are mentioned in tables.

Table 4. *Interatomic distances and bond angles in cadmium nitrate tetrahydrate group*

Standard errors are given in parenthesis.

Cd-OH <sub>2</sub> distances		O-OH <sub>2</sub> distances	
Cd(1·00)-O(5·00)	2·26 (0·02) Å	O(2·00)-O(6·00)	2·82 (0·02) Å
Cd(1·00)-O(6·00)	2·33 (0·02)	O(2·00)-O(5·00)	3·00 (0·03)
		O(3·00)-O(5·01)	3·07 (0·03)
		O(3·00)-O(6·01)	3·10 (0·04)
		O(2·00)-O(6·01)	3·18 (0·03)
		O(3·00)-O(5·00)	3·25 (0·03)
Cd-O (from NO <sub>3</sub> ) distances		H <sub>2</sub> O-OH <sub>2</sub> distances	
Cd(1·00)-O(2·00)	2·44 (0·02) Å	O(5·00)-O(5·01)	3·19 (0·04) Å
Cd(1·00)-O(3·00)	2·59 (0·02)	O(5·00)-O(6·00)	3·32 (0·03)
		O(6·00)-O(6·01)	3·34 (0·04)
Cd-N distance		O-N-O angles in NO <sub>3</sub> group	
Cd(1·00)-N(7·00)	2·93 (0·02) Å	O(2·00)-N(7·00)-O(3·00)	116·4° (2·1°)
		O(2·00)-N(7·00)-O(4·00)	129·7 (2·3)
		O(3·00)-N(7·00)-O(4·00)	112·7 (2·1)
O-N distances in NO <sub>3</sub> group		O-Cd-O angles in Cd polyhedron	
O(2·00)-N(7·00)	1·21 (0·03) Å	O(2·00)-Cd(1·00)-O(3·00)	48·9° (0·7°)
O(3·00)-N(7·00)	1·25 (0·03)	O(6·00)-Cd(1·00)-O(2·00)	72·5 (0·6)
O(4·00)-N(7·00)	1·26 (0·03)	O(6·00)-Cd(1·00)-O(3·01)	77·9 (0·9)
		O(5·00)-Cd(1·00)-O(3·01)	78·1 (0·9)
		O(5·00)-Cd(1·00)-O(2·00)	79·5 (0·8)
		O(6·00)-Cd(1·00)-O(2·01)	83·8 (0·7)
		O(5·00)-Cd(1·00)-O(3·00)	83·9 (0·9)
		O(5·00)-Cd(1·00)-O(5·01)	89·8 (1·2)*
		O(6·00)-Cd(1·00)-O(6·01)	91·5 (1·1)*
		O(5·00)-Cd(1·00)-O(6·00)	92·6 (0·8)
		O(6·00)-Cd(1·00)-O(3·00)	121·1 (0·8)
		O(5·00)-Cd(1·00)-O(2·01)	126·6 (0·7)
		O(2·01)-Cd(1·00)-O(3·00)	141·8 (0·7)
		O(2·00)-Cd(1·00)-O(2·01)	146·0 (1·1)*
		O(3·00)-Cd(1·00)-O(3·01)	154·6 (1·6)*
		O(5·00)-Cd(1·00)-O(6·01)	160·7 (0·7)
H <sub>2</sub> O-N distances			
O(5·00)-N(7·00)	3·39 (0·02) Å		
O(6·00)-N(7·00)	3·94 (0·03)		
O-O distances between NO <sub>3</sub> oxygens			
O(2·00)-O(3·00)	2·09 (0·03) Å		
O(3·00)-O(4·00)	2·09 (0·03)		
O(2·00)-O(4·00)	2·24 (0·03)		

\* All values of O-Cd-O angles, except those designated by asterisks, appear twice in the polyhedron.



of neighboring molecules have a range of values increasing from 2.87 Å. These distances between nitrate-oxygen and water-oxygen atoms or between water-oxygen atoms indicate possible hydrogen bonding between the atoms of neighboring cadmium nitrate tetrahydrate groups. Further evidence is provided by the list of angles around water molecules also given in Table 6. These angles, selected because their values were close to the HOH bond angle in H<sub>2</sub>O, may be used in conjunction with the distances to select possible hydrogen bond locations. Based on the distances and angles hydrogen bonds are probably between O(4.24)–O(5.00)–O(6.06) and O(3.69)–O(6.00)–O(2.11) atoms.

Table 6. Selected angles involving water oxygen atoms

O(5.11)–O(5.00)–O(2.06)	102.8° (0.5°)
O(4.24)–O(5.00)–O(6.06)	104.1 (1.1)
O(4.24)–O(5.00)–O(6.00)	104.2 (1.0)
O(3.69)–O(6.00)–O(2.11)	103.2 (0.9)
O(5.46)–O(6.00)–O(4.69)	104.8 (1.0)
O(4.69)–O(6.00)–O(4.11)	105.0 (0.6)

The values of the intermolecular distances obtained during this refinement are not significantly different from the results obtained before. The cadmium–oxygen distances, obtained after refinement, are a little shorter than reported previously. The shortest one is 2.26 Å. This length is 0.09 Å shorter than the cadmium–oxygen distance in CdO which has a sodium chloride structure (Wyckoff, 1963). The values of two shorter cadmium–oxygen distances (2.26 and 2.33 Å) are also in good agreement with those already found in other cadmium compounds; e.g. the cadmium–oxygen distance in monomethylureacadmium chloride is 2.18 Å, in bisacetamide-cadmium chloride is 2.23 Å, in bisthiourea-cadmium formate is 2.28 Å, in bisurea-cadmium chloride is 2.28 Å and in bisbiuret-cadmium chloride is 2.34 Å (Nardelli, Fava-Gasparri & Boldrini, 1965). A still

shorter cadmium–oxygen (water) distance of 2.12 Å was found in the structure of tricadmium sulphate octahydrate (Lipson, 1936). For comparison, in this structure the distances of six nearest atoms (four sulphate oxygen atoms and two from water molecules) located around the cadmium atom vary from 2.12 to 2.63 Å. In the structure of cadmium nitrate tetrahydrate the distances of eight nearest atoms (four from water molecules and four nitrate oxygens) around the cadmium atom range from 2.26 to 2.59 Å. The distances in the NO<sub>3</sub> group do not deviate significantly from the results obtained before and are in agreement with the known data (*International Tables for X-ray Crystallography*, 1962). The O–N–O angles in the NO<sub>3</sub> groups indicate that the nitrogen atom lies in the plane of the oxygen triangle within the error of experiment.

We would like to thank Dr R. Willett for his instructive help during the calculations, the Washington State University Computing Center for a grant of computing time, and the U.S. Atomic Energy Commission for partial support of this work.

#### References

- BUSING, W. R., MARTIN, K. O. & LEVY, H. A. (1962). U.S. Atomic Energy Commission Report ORNL-TM-305.  
 BUSING, W. R., MARTIN, K. O. & LEVY, H. A. (1964). U.S. Atomic Energy Commission Report ORNL-TM-306.  
 HUGHES, E. W. (1941). *J. Amer. Chem. Soc.* **63**, 1737.  
*International Tables for X-ray Crystallography* (1962). Vol. III. Birmingham: Kynoch Press.  
 LIPSON, H. (1936). *Proc. Roy. Soc. A*, **156**, 462.  
 MATKOVIĆ, B. & RIBAR, B. (1963). *Croat. Chem. Acta*, **35**, 147.  
 NARDELLI, M., FAVA-GASPARRI, G. & BOLDRINI, P. (1965). *Acta Cryst.* **18**, 618.  
 WYCKOFF, R. W. G. (1963). *Crystal Structures*, Vol. I, p. 86. New York: John Wiley.  
 ZELENKO, B. & ZAKRAJŠEK, E. (1964). Private communication.